Controlling Lateral Fano Interference Optical Force with Au–Ge$_2$Sb$_2$Te$_5$ Hybrid Nanostructure

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* Supporting Information

ABSTRACT: We numerically demonstrate that a pronounced dipole–quadrupole (DQ) Fano resonance (FR) induced lateral force can be exerted on a dielectric particle 80 nm in radius (R$_{\text{sphere}}$ = 80 nm) that is placed 5 nm above an asymmetric bow-tie nanoantenna array based on Au/Ge$_2$Sb$_2$Te$_5$ dual layers. The DQ-FR-induced lateral force achieves a broad tuning range in the mid-infrared region by changing the states of the Ge$_2$Sb$_2$Te$_5$ dielectric layer between amorphous and crystalline and in turn pushes the nanoparticle sideways in the opposite direction for a given wavelength. The mechanism of lateral force reversal is revealed through optical singularity in the Poynting vector. A thermal–electric simulation is adopted to investigate the temporal change of the Ge$_2$Sb$_2$Te$_5$ film’s temperature, which demonstrates the possibility of transiting the Ge$_2$Sb$_2$Te$_5$ state by electrical heating. Our mechanism by tailoring the DQ-FR-induced lateral force presents clear advantages over the conventional nanoparticle manipulation techniques: it possesses a pronounced sideways force under a low incident light intensity of 10 mW/μm$^2$, a fast switching time of 2.6 μs, and a large tunable wavelength range. It results in a better freedom in flexible nanomechanical control and may provide a new means of biomedical sensing and nano-optical conveyor belts.

KEYWORDS: phase change material, Fano resonance, optical manipulation, surface plasmons, optical force

Optomechanical manipulation of biomolecules using a focused laser beam has led to a host of applications in the biological and physical sciences. 1,2 Even so, scaling this approach to nanoparticles is difficult since the limit of diffraction gives an upper bound in the gradient along light intensity and thus restrains the maximum gradient force that is proportional to the scale of the specimens for a given input power. 3 Since the optical trapping force increases with the local field gradient, nanostructures employed as auxiliary tools for optical trapping have been proposed to enhance the electromagnetic (EM) field and generate an evanescent field that gives a huge field gradient within a subwavelength area, e.g., slot waveguides, 4 whispering-gallery-mode resonators, 5 and photonic systems. 6,7 Particularly, plasmonic optical tweezers are shown to be an influential approach to shrink the traditional optical tweezers to subwavelength scale. 8–10 This scheme can break the diffraction limit since the optical trapping is based on localized surface plasmon resonance (LSPR) instead of propagating an EM wave. The LSPR mode confines the light within the diffraction limit, thus trapping the nanoparticle. Moreover, the LSPR mode’s origin is the exponential decay of EM fields at the interface of the metal and dielectric, hence significantly enhancing the optical force caused by an intense field gradient. This leads to an achievement of stable optical trapping under a low incident light intensity. 11–13 Therefore, plasmonic nanostructures such as nanorods, 14 nanocavities, 15 bow-tie nanoantennas, 16 and coaxial apertures 17 have been proposed to generate gradient optical force to trap molecules a few tens of nanometers in scale. The previous efforts commonly assumed that light could trap molecules using conservative gradient force induced by either bulky optical setups or compact nanodevices, whereas the position control of the nanoparticle in the plane perpendicular to the incident light using the conservative lateral force is rarely investigated.

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Lately there is a growing attention to sensitive probing and enantiomer-selective separation of a racemic mixture through chiral forces. Even so, these strategies require circularly polarized light, which is more complicated to employ in comparison with linearly polarized light. Very recently, it has been shown that a plane wave with linear polarization can provide a nonconservative lateral force that drags nanosize helical specimens with different handedness along opposite directions. However, the majority of studies of laterally nonconservative optical force aim at pushing chiral particles sideways, while the conservative lateral force on achiral particles and its application on optical manipulation are rarely investigated, such that the trace of a nonchiral particle changes at the molecular scale along the direction perpendicular to the incident light, which can behave as an optical conveyor belt to trap dielectric particles at different positions under controllable conditions.

Fano resonance (FR) can be understood as an interaction between a system with a broadened resonant line width and a system with a narrow resonance. FRs have been unveiled not only in a variety of plasmonic nanostructures but also in magnetodielectric ones. Despite its potential applications in nanoantennas, sensing and optoelectronic devices, modern trends propose to study the dipole–quadrupole (DQ) FR induced optical binding force between plasmonic resonators. The direction of OBF is perpendicular to the incident light and can be reversed by tuning the geometrical size and gap of the resonators. Inspired by these interesting phenomena, one important question arises: can we reverse the direction of the lateral force acting on nonchiral nanoparticles that is placed above the plasmonic nanostructure exhibiting DQ-FR.

Bow-tie nanoantennas (BNAs) have shown advantages over high numerical aperture (NA) lenses for optical trapping since they combine large field enhancements and subdiffraction field confinement properties within nanogaps through the LSPR. In this work, we numerically demonstrate an ultrafast reversible position controlling of nanoparticles using an actively tuned lateral DQ-FR force that is generated by an array of asymmetric BNAs embedded in a prototypical phase change material (Ge2Sb2Te5) dielectric layer. The BNAs are designed to support a DQ-FR by introducing an asymmetry in the two tailored Au triangles to excite the nonradiative quadrupole mode. Unlike most prior plasmonic tweezers, here we will show that the DQ-FR in the asymmetric BNAs will induce a conservative lateral force that pushes the nanoparticles sideways rather than trap them. Moreover, the lateral optical force is reversibly altered, through a switchable tuning of the DQ-FR wavelength achieved by varying the state of Ge2Sb2Te5 between amorphous and crystalline. Consequently, it can change the sign of DQ-FR-induced transverse force at a fixed wavelength, hence moving the particle in the opposite direction. This advantage leads to a reversible manipulation of nanoparticles at linearly polarized plane wave incidence.

In our work, we show the DQ-FR-induced transverse force is related with the optical singularity in the Poynting vector (S). We explore the origin of transverse force as a result of a distinctive energy flow. It has been presented that the conservative lateral force is reversed via the manipulation of the distribution of singular points, which leads to a displacement of the hot spot around the nanoparticle, and the variation of the singular point distribution is obtained by a switchable state change of Ge2Sb2Te5. Just as crucially, a thermoelectric simulation is performed to investigate the temporal change of the temperature of the Ge2Sb2Te5 dielectric layer. It illustrates that the amorphous Ge2Sb2Te5 layer’s temperature can be increased from 293 K to 433 K (state change point of Ge2Sb2Te5) in 2.6 μs, under a biasing voltage of 20 V. Thereby our proposed BNAs can rapidly alter the direction of DQ-FR-induced lateral force, which is very advantageous for biomedical applications where ultrafast manipulation of nano-objects is a key concern.

## RESULTS AND DISCUSSION

The proposed BNA has two 15 nm thick Au isosceles triangles, the tip-to-base height of each triangle is 160 nm, and the two triangles are placed tip-to-tip and spaced by a small distance of 10 nm to generate a strong near-field intensity with an intense field gradient. The BNAs are deposited on a 15 nm thick Ge2Sb2Te5 dielectric layer. Herein, we model two sets of BNAs starting from a symmetric resonator with two exactly the same isosceles triangles, where the tip angle of each triangle is θt = 5° (Figure 1a), and then increase the tip angle of the right

![Figure 1](image-url)

**Figure 1.** Schematic of a three-dimensional view of (a) symmetric BNAs and (b) asymmetric BNAs composed of Au BNAs embedded in the Ge2Sb2Te5 dielectric layer sitting on a BK7 glass substrate. A linearly polarized light from the top illuminates the structures. Right columns in (a) and (b) are the top view of the meta-atom. Illustration of the action of a dielectric sphere (n_sphere = 2, R_sphere = 80 nm) in an asymmetric BNA optical system for the (c) amorphous state and (d) crystalline state. Blue arrows indicate the directions of the spheres’ motions.

isosceles triangle to θt = 25° to break the symmetry (Figure 1b). For both structures, the lattice constant of the BNAs is L = 380 nm and the Au bow-tie antennas are periodically placed in the x and y directions. The BNAs embedded in the Ge2Sb2Te5 dielectric layer are considered to stand on a BK7 glass substrate. Au is used as the metal owing to its nonoxidation and low ohmic loss. The geometry of the asymmetric bow-tie antenna and the Ge2Sb2Te5 layers’ thickness are selected to allow for exerting a pronounced DQ-FR-induced lateral force on a dielectric particle (R_sphere = 80 nm), placed 5 nm above the
surface of the asymmetric BNAs under a low illumination intensity of 10 mW/μm² for both amorphous (Figure 1c) and crystalline (Figure 1d) states, respectively. To approach a real situation, the system is placed in an environment of water. The dielectric particle (\(n_{\text{sphere}} = 2\)) is used for mimicking biological particles, such as proteins and viruses. Noted that, here, the dielectric nanosphere is neither plasmonic nor magnetodielectric; in other words the FRs considered in the model originate purely from the plasmonic BNA. The structures are calculated via commercial software (Lumerical FDTD Solutions) based on the finite difference time domain (FDTD) method. The size of the uniform mesh is set at 3 nm along all Cartesian axes (Δx = Δy = Δz = 3 nm) in order to minimize the numerical errors. Perfectly matched layer (PML) boundary conditions are used along the z direction and periodic boundaries along the x and y directions. This model is used to achieve the EM field distribution around the targeting particle to calculate the optical force. A Drude model is employed for the dielectric permittivity of Au, \(\varepsilon_{\text{Au}}(\omega) = 1 - \frac{\omega_p^2}{\omega^2 + i\omega \Gamma}\)

where \(\omega_p = 1.37 \times 10^{16} \text{ rad/s}\) is the plasma frequency and \(\alpha_s = 4.08 \times 10^{15} \text{ rad/s}\) is the scattering frequency for Au.6 The structures are excited by a linearly polarized plane wave having a range of wavelengths from 1000 to 5000 nm, propagating through the z direction with the E-field polarized in the transverse axis (x axis) of the bow-tie antenna (Figure 1).

Ge\(_2\)Sb\(_2\)Te\(_5\) is a chalcogenide glass having a crystallization temperature of \(\sim 433 \text{ K}\) and a melting temperature of \(\sim 873 \text{ K}\). The amorphous Ge\(_2\)Sb\(_2\)Te\(_5\) dielectric interlayer will be crystallized by heating it above the crystallization temperature, but without obtaining the melting temperature. A femtosecond (fs) laser with a relatively high power may amorphize the Ge\(_2\)Sb\(_2\)Te\(_5\) subsequently thermalizes and melts. Fast cooling quenches the melt into the amorphous state. It is because the fs laser generates a very high density of electron−hole pairs in the Ge\(_2\)Sb\(_2\)Te\(_5\) that the Ge\(_2\)Sb\(_2\)Te\(_5\) subsequently thermalizes and melts. Fast cooling quenches the melt into the amorphous state. Thus, Ge\(_2\)Sb\(_2\)Te\(_5\) has a potential of realizing modulation functionality, as it can reversibly switch between crystalline and amorphous states in the infrared region.54−58 The dielectric constant of Ge\(_2\)Sb\(_2\)Te\(_5\) for the mid-infrared (M-IR) range is presented in Supplementary Section S1.

The force acting on a dielectric particle located in time-harmonic EM fields can be attained through a linear momentum conservation, in which the linear momentum is either mechanical or electromagnetic. The sum of these two momentums is preserved. When a particle is illuminated under a light, the momentum is transferred from the optical field to the mechanical and thus leads to an optical force exerted on the particle. Therefore, the optical force relates to the variation of mechanical momentum (p) with time (dp/dt). The EM-field momentum flux in the linear medium of permittivity \(\varepsilon\) and permeability \(\mu\) is shown by the time-averaged Maxwell stress tensor (\(\mathbf{T}\)).

\[
\langle \mathbf{T} \rangle = \frac{1}{2} \mathbf{Re} \left[ \varepsilon \mathbf{E} \mathbf{E}^* + \mu \mathbf{H} \mathbf{H}^* - \frac{1}{\omega} (\mathbf{E} \mathbf{H}^T + \mathbf{H} \mathbf{E}^T) \right]
\]

where \(\langle ... \rangle\) represents \(\frac{1}{T} \int_0^T ... \, dt\) with \(T = \frac{2\pi}{\omega}\), \(\mathbf{HH}^*\) and \(\mathbf{EE}^*\) the outer product of the fields, and \(\mathbf{I}\) the matrix of identity.

The total time-averaged FR induced force \((F_{\text{total}})\) exerted on the sphere is calculated using the Maxwell stress tensor formalism and is given by

\[
F_{\text{total}} = \int \langle \mathbf{T} \rangle \hat{n} \, dS
\]

where \(\hat{n}\) is the unit vector normal to the surface and \(d\) the integration calculated over a closed surface that surrounds the bead. Here, an FDTD model is built up to calculate the EM fields at the surface of a square box surrounding the dielectric bead.

Figure 2a presents reflectance for the structures of symmetric and asymmetric BNAs under normal incidence, where the state of the Ge\(_2\)Sb\(_2\)Te\(_5\) dielectric is amorphous. Here, we show that the symmetric BNAs exhibit a strong reflectance response with a resonant wavelength centered at 2788 nm (shown as a black dotted curve). By increasing the tip angle of the right triangle to \(\theta_1 = 25^\circ\), the primary plasmon resonant mode for the symmetric BNAs breaks into two distinct resonant peaks at 1963 and 2727 nm by an asymmetric resonant dip at 2458 nm (shown as a red solid curve). In the case of the highly symmetric BNAs, only a bright dipolar mode that is strongly radiative in nature is excited. It is because the resonant modes in the two equal Au triangles overlap that they oscillate in phase and interfere constructively. In the asymmetric BNAs, a dark quadrupole mode is excited, which leads to a destructive interference between the bright dipolar mode of the small triangle (\(\theta_1 = 5^\circ\)) and dark quadrupole mode of the large triangle (\(\theta_2 = 25^\circ\)). The coherent coupling between the bright dipolar mode and dark quadrupole mode cancels the polarization of the bright dipolar mode, making a DQ-FR dip at 2458 nm. We show that the enhanced FR can be achieved for the asymmetric BNAs since it possesses an ability to easily tune the dipolar and quadrupolar resonances by...
varying the geometry of the triangle, which determines the coupling strength between the neighboring plasmon modes in the bow-tie antenna. Figure 2c presents the intensity distribution of the total E-field $E = \sqrt{E_x^2 + E_y^2 + E_z^2}$ in the $x$-$y$ plane along the Au/water interface at $\lambda = 2788$ nm (denoted as the $P_1$ mode) in the symmetric BNAs with amorphous Ge$_2$Sb$_2$Te$_5$, where the color demonstrates the E-field intensities’ magnitude. This shows that the distribution of the E-field intensity is symmetric and mainly concentrates within the tips of the bow-tie antenna. This indicates that the charges in the two equal bow-tie antennas oscillate in phase and interfere constructively (namely, the charges in the left and right tips of the gap are the same). Figure 2d demonstrates the E-field intensity distribution at $\lambda = 2727$ nm (denoted as the $P_2$ mode) for the asymmetric BNAs with amorphous Ge$_2$Sb$_2$Te$_5$. The E-field intensity distribution at the $P_2$ mode is more efficiently localized in the tip of the left, smaller triangle. Figure 2c shows the asymmetric BNAs also support the large E-field intensity in the tip of the right, larger triangle at the resonant wavelength of $\lambda = 1963$ nm (denoted as the $P_3$ mode). As can be seen, the asymmetric BNAs provide the stronger electric resonances at the $P_2$ and $P_3$ modes compared to the $P_1$ mode in the symmetric BNAs. This is because, at the resonant mode of the asymmetric BNAs (i.e., DQ-FR), the charges in the left and right tips of the gap are opposite (namely, the charges in the two different bow-tie antennas oscillate out-of-phase and destructively interfere), which not only enhances the E-field intensity in the gap of the bow-tie nanoantenna but also resolves nanoscale mode volumes. Therefore, a laterally conservative optical force acting on a nanobead above asymmetric BNAs is larger than the symmetric BNAs, owing to the existence of the DQ-FR. Figure 2b shows the evolution of the DQ-FR in reflectance spectra of the asymmetric BNAs as transiting the state of Ge$_2$Sb$_2$Te$_5$ from amorphous to crystalline. With state variation of Ge$_2$Sb$_2$Te$_5$, the DQ-FR dip at $\lambda = 2458$ nm with an amorphous phase red-shifts to 3395 nm with a crystalline state. This is because a significant variation in $\text{Re}(\epsilon_1(\omega))$ (a real part of dielectric permittivity $\epsilon_1(\omega)$) of Ge$_2$Sb$_2$Te$_5$ across the M-IR region is attained after altering the phase of thin film’s structure from the amorphous to crystalline (Supplementary Section S1). This leads to a variation of the environmental dielectric constant of the BNAs and, in turn, tunes the spectra of the DQ-FR. Due to this large tuning range, the proposed phase-changed BNAs can be very useful in modulating the DQ-FR effect and sequentially provides a significant change of sign of the DQ-FR induced conservative lateral force at 2680 nm, as shown in Figure 3d.

The total optical force $F_{\text{total}}$ can be resolved into two components: one is antiparallel or parallel to the propagation direction of incidence; the other is normal to the direction of the incidence, the so-called lateral optical force. In this work, we are focused on the lateral forces along the $x$ axis ($F_x$), acting on the nonmagnetodielectric dielectric sphere ($R_{\text{sphere}} = 80$ nm) placed 5 nm above the asymmetric plasmonic BNAs with Ge$_2$Sb$_2$Te$_5$. Here the main variables to be determined are the tip angles of $\theta_1$ and $\theta_2$ shown in Figure 1b. They are optimized for obtaining the maximum difference of $F_x$ between the amorphous and crystalline BNAs at a fixed wavelength of $\lambda = 2680$ nm. Figure 3a and b show 2D diagrams of $F_x$ against $\theta_1$ and $\theta_2$ for both the amorphous and crystalline structures, respectively, where the $F_x$ transits from $-1.2$ to 0.9 pN with $\theta_1 = 5^\circ$ and $\theta_2 = 25^\circ$. To investigate how the $F_x$ is induced by the DQ-FR, Figure 3d presents the comparison of the spectra of $F_x$ between the amorphous and crystalline phases. As presented by the red solid line in Figure 3d, for the amorphous asymmetric BNAs, the DQ-FR provides an asymmetric line shape in the spectra of the $F_x$. The $F_x$ is evident and undergoes a positive DQ-FR-induced lateral force ($F_x > 0$) across the blue region of the DQ-FR of

Figure 3. 2D diagram of lateral optical forces ($F_x$) against $\theta_1$ and $\theta_2$ at a fixed wavelength of 2680 nm, where the $F_x$ is exerted on the dielectric sphere ($R_{\text{sphere}} = 80$ nm) placed 5 nm above the asymmetric BNAs (a) with amorphous Ge$_2$Sb$_2$Te$_5$ and (b) with crystalline Ge$_2$Sb$_2$Te$_5$; (c) 2D diagram of the difference of the $F_x$ ($\Delta F_x$) between the amorphous and crystalline asymmetric BNAs against $\theta_1$ and $\theta_2$ at a fixed wavelength of 2680 nm; (d) comparison of the spectra of the $F_x$ between the amorphous and crystalline asymmetric BNAs with $\theta_1 = 5^\circ$ and $\theta_2 = 25^\circ$. DOI: 10.1021/acsphotonics.6b00448

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\( \lambda_{Fano} = 2214 \text{ nm} \) (the wavelength at which \( F_x \) crosses the zero point, \( F_x \) repels the particle toward the \(+x\) direction. For \( \lambda > \lambda_{Fano} \), \( F_x \) changes from positive to negative (\( F_x < 0 \)) to drag the particle along the \(-x\) direction. Namely, \( F_x \) can be reversed when the wavelength of the incident plane wave increases from 1000 to 5000 nm. Moreover, the \( F_x \) exhibits a profoundly asymmetric resonance dip around \( \lambda = 2680 \text{ nm} \), indicating a strong negative force (\( F_x = -1.2 \text{ pN} \)) under a low incident intensity of 10 mW/\( \mu \text{m}^2 \). To explore why \( F_x \) at \( \lambda = 1938 \text{ nm} \) is larger than that at \( \lambda = 2646 \text{ nm} \) (shown in Figure 3d), we present the \( E \)-field intensity distribution in Supplementary Section S2.

Transiting the phase of Ge\(_2\)Sb\(_2\)Te\(_5\) from amorphous to crystalline (shown as a cyan solid line) spectrally tunes the DQ-FR in the asymmetric phase-changed BNAs, hence red-shifting the dip of \( F_x \) from 2680 to 3550 nm. It is noteworthy that around the wavelength of 2680 nm, \( F_x \) changes sharply in the opposite direction for the amorphous asymmetric BNAs (\( F_x = -1.2 \text{ pN} \)) and crystalline BNAs (\( F_x = 0.9 \text{ pN} \)). Therefore, reversibly switching the state of Ge\(_2\)Sb\(_2\)Te\(_5\) between amorphous and crystalline can change the signs of the \( F_x \) exerted on the nanoparticle and, in turn, laterally manipulates the particle in the reverse direction. The higher order multipolar modes (the mode’s order is higher than quadrupole) can also be excited in the right, large triangle (\( \theta_1 = 25^\circ \)) to interfere with the dipolar mode in the left, small triangle (\( \theta_1 = 5^\circ \)) and generate higher order FR. However, here these higher order modes’ influence on the \( F_x \) is neglected. The octupole resonance is comparatively weak due to the ultrasmall beads. Thereby, the optical forces induced by the higher order FR are not pronounced in the spectra of \( F_x \) for the nanoparticles, and the quadrupole mode is enough for the convergence. To show the DQ-FR-induced \( F_x \) agrees well with a Fano model, we approach the curve of \( F_x \) acting on the dielectric sphere above both the amorphous and crystalline asymmetric BNAs, respectively, using the FR line shape in refs 26 and 27, as we demonstrate in Supplementary Section S3.

The lateral force induced by Fano interactions comes from the divergence of EM energy density, where the asymmetric BNAs are selected to concentrate the \( E \)-field to a very localized and intense hot spot, providing a large force density.\(^{28,29}\) Such a strong near-field hot spot leads to a pronounced enhancement in EM field strength and its gradient within this region.\(^{25,28}\) Therefore, the ability to control the location of hot spots by changing the state of Ge\(_2\)Sb\(_2\)Te\(_5\) between the crystalline and amorphous enables one to switch the direction of DQ-FR-induced lateral conservative force. To investigate the relation between the lateral force \( F_x \) and near-field hot spot, the near-field Poynting vector \( \langle S \rangle \) is demonstrated when the dielectric sphere is positioned 5 nm above the center of an asymmetric BNA for both crystalline and amorphous phases, respectively. \( S \) can provide an intuitive physical explanation of the matter-wave interference, wherein \( S \) represents the flow of energy referring to the Poynting theorem.\(^{50}\) The first investigation of wavefront dislocations was performed by Nye and Berry.\(^{61}\) Lately, the optical singularities in \( S \) have been applied to study the underlying physics of distinctively optical micromanipulation.\(^{62}\) Crucially, FR and optical singularity are in fact closely interrelated.\(^{63}\) Therefore, the energy flux trajectories and optical singularity topology are enlightening to interpret the fundamental mechanism of QD-FR-caused force on the nanosphere. One can categorize the singular points of \( S \) as vortex, saddle, sink, focus, and node.\(^{64,65}\) The flows of energy vary with distributions of singular points and thus change the force acting on the nanoparticles. The streamlines of \( S \) and distributions of near-field singularities in the \( x-z \) plane are illustrated in Figure 4, in order to expose the hot spot map. The blue arrows and color bars represent the directions and logarithmic modulus of \( S \), accordingly. The streamline (black solid line) derives from a solution of \( \frac{dr}{d\phi} = r \frac{\langle S \rangle_\phi}{\langle S \rangle_r} \), where \( \langle S \rangle_\phi \) and \( \langle S \rangle_r \) are the constituents of \( \langle S \rangle \) in polar coordinates.\(^{66}\) The \( S \) in the amorphous asymmetric BNA at \( \lambda = 2680 \text{ nm} \) is shown in Figure 4a. It shows that the hot spot is created at the tip of the left triangle of the BNAs. The field gradient near the hot spot results in a net \( F_x \) toward the \(-x\) direction (\( F_x < 0 \), red solid line in Figure 3d). In the vicinity of the tips of triangles, two pairs of saddle-vortex singularities appear. The saddle and vortex points unveil the significant variations in energy flow close to them. For example, the vortex points (marked with 1 and 3) “trap” the energy flux inside the whirlpool areas, and the saddle points (marked with 2 and 4) “seize” the energy flux from the surroundings. The LSPRs constructively interact with the incident light, creating a circle around vortex point 1. Although vortex 3 and saddle 4 form a pair of saddle-vortex to direct the lightwave from the surroundings toward the bead’s right side, the light energy is not pronouncedly improved. This is because the light passing through the right side of the sphere is guided to the left side through saddle 2 and encircles vortex 1. Consequently, the singular points may attract, guide, and congregate the light toward the tip of the right triangle and thus provides a hot spot.

For the crystalline BNA at \( \lambda = 2680 \text{ nm} \), Figure 4b shows the hot spot is shifted to the tip of the right triangle, thus altering the sign of \( F_x \) (\( F_x > 0 \), cyan solid line in Figure 3d). On the tip of the right triangle, a vortex point is created (marked with 7) to concentrate the \( E \)-field within the whirlpool region. Meanwhile a vortex-saddle pair (marked with 5 and 6) are excited on the tip of the left triangle. However, the lightwave travels across saddle point 6, forms loops at vortex point 5, returns to saddle point 6, and propagates to vortex point 7. Therefore, the energy in the right side is stronger than that in the left side, resulting in a hot spot and thus a net lateral force along the \(+x\) axis (\( F_x > 0 \)).
Considering the random Brownian motion of nanoparticles in water, the stability of a nanoparticle must be examined. The dielectric particle’s motion is modeled by the Langevin equation:

\[
\begin{align*}
\frac{d^2 x(t)}{dt^2} &= -\frac{\beta}{m} \frac{dx(t)}{dt} + \frac{\zeta}{m} W_x(t) + \frac{F_x(x,y)}{m} \\
\frac{d^2 y(t)}{dt^2} &= -\frac{\beta}{m} \frac{dy(t)}{dt} + \frac{\zeta}{m} W_y(t) + \frac{F_y(x,y)}{m} 
\end{align*}
\]

(3)  

(4)

where \(x(t)\) and \(y(t)\) are the particle’s positions, \(F_x(x,y)\) and \(F_y(x,y)\) are the lateral forces, \(W_x(t)\) and \(W_y(t)\) are the stochastic noise terms that model random collisions from fluid molecules along both the \(x\) direction and \(y\) direction, respectively, \(m\) is the sphere’s mass, \(\beta = 6\pi \eta R_{\text{sphere}}\) is the drag coefficient (from Stokes’ law for a spherical particle), and \(\eta = 0.89\ \text{mPa}\cdot\text{s}\) is the viscosity of water. The scaling constant for the stochastic noise term is given by \(\zeta = \sqrt{2\beta k_b T}\) where \(k_b\) is Boltzmann’s constant and \(T = 300\ \text{K}\). The simulation algorithm was run for a total of 200 000 time steps with a very short time step of 1 ns. Here, in order to simplify the simulation, we did not consider the influence of optical force along the \(z\) direction on the motion of the particle.

In Figure 5a, we dynamically simulated the stability of nanoparticles by observing time sequences of the movements of a dielectric sphere that is placed 5 nm above the asymmetric BNA with amorphous Ge\(_2\)Sb\(_2\)Te\(_5\), respectively. The particle in two dimensions (\(x-y\) plane) is tracked with nanometer precision. The intensity of the beam is 10 mW/\(\mu\)m\(^2\) with an excitation wavelength of \(\lambda = 2680\ \text{nm}\). A 0.2 ms trajectory of the sphere above the asymmetric BNA with amorphous Ge\(_2\)Sb\(_2\)Te\(_5\) is shown by the red solid line. Owing to the location of the hot spot around the left tip of the triangle (see Figure 4a), a lateral force \(F_x\) is generated along the \(-x\) axis \((F_x < 0)\) and thus causes a motion of the particle to the left (Supplementary Movie S1). In contrast, within illumination by the plane wave beam, the nanoparticle above the crystalline structure follows the opposite direction of motion (see cyan solid line). This is because the hot spot shifted to the tip of the right triangle (see Figure 4b), where the \(F_x\) generates along the +x axis \((F_x > 0)\), hence pushing the particle to the right (Supplementary Movie S2).
The position control of the spheres along the amorphous and from the work of R dipolar and quadrupolar modes causes a prominent nm for transit from the dip to peak at 0.2 ms. As can be seen in both Figure 5a and the supplementary movies, the nanoparticles thermally fluctuate only from −10 to 5 nm for the amorphous and from −8 to 14 nm for the crystalline state along the y axis, which would not significantly affect the lateral position control of the spheres along the x axis. The particles are stably trapped at the position of blue circles at the end of 0.2 ms.

In Figure 5b, we show the transverse optical potential $U_0 = k_f T$ created by the BNA for the nanoparticles ($R_{\text{sphere}} = 80$ nm) at different positions along the x axis, where $T = 300$ K is the temperature of environmental water. The optical potential $U_0$ is the work of $F_r$ moving the particle from the central gap of the BNA to its arm along the x axis. In the coordinate system, $F_r$ can provide a negative potential well ($U_0 < 0$). For the asymmetric BNA with amorphous Ge$_2$Sb$_2$Te$_5$, $U_0$ is negative ($U_0 < 0$) along the −x axis (see red solid line in Figure 5b), and a steep potential valley appears at $x = −66$ nm corresponding to the potentials of DQ interference induced Fano lateral forces. Such a potential valley can drag the nanoparticle toward the left arm of the BNA and stably trap the nanoparticle around $x = −66$ nm (indicated by a purple dot). On transiting the state of Ge$_2$Sb$_2$Te$_5$ from amorphous to crystalline, the potential valley of $U_0$ occurs at $x = +38$ nm, relating to the DQ-FR-induced $F_r$ (see cyan solid line in Figure 5b). Thus, the particle can be dragged to the right arm of the BNA and finally captured around $x = +38$ nm.

Furthermore, we investigate that such an asymmetric BNA can also produce a strong $F_r$ acting on the nanoparticle with a range of the radius from 50 to 80 nm owing to the DQ-FRs. As can be seen in Figure 6a–d, the Fano interaction between the dipolar and quadrupolar modes causes a prominent $F_r$ that can transit from the dip to peak at $\lambda = 2635$, 2646, 2668, and 2680 nm for $R_{\text{sphere}} = 50, 60, 70, \text{and 80 nm}$, respectively, when the state of Ge$_2$Sb$_2$Te$_5$ switches between the amorphous and crystalline. Although the absolute value of $F_r$ decreases with $R_{\text{sphere}}$, $F_r$ still changes from −0.5 to +0.6 pN ($\Delta F_r = 1.1$ pN) for the smallest particle ($R_{\text{sphere}} = 50$ nm) during the phase transition, which is sufficient for the optical manipulation of the nanoparticles.

The most intriguing property of chalcogenide (i.e., Ge–Sb–Te) plasmonics is its ultrabroad and fast tunability. One important concern for its practical applications is the response time of tunability. Recently, people have put much effort into shortening the time of state change in Ge–Sb–Te and experimentally demonstrated the prospect of acquiring a speed quicker than 100 ns. These pave the way to ultrafast tuning of the Ge–Sb–Te, which can provide a new scheme to obtain an immediate real-time position control of the specimen.

Electrical heating can be employed to achieve a reversible crystalline–amorphous phase change in Ge$_2$Sb$_2$Te$_5$. Thus, it is important to study the switching behavior of asymmetric phase-change BNAs induced by electrical heating. Here, an alternative modeling approach has been developed on the basis of the finite element method (FEM) solver within COMSOL. First, the asymmetric BNAs based on amorphous Ge$_2$Sb$_2$Te$_5$ are set up in COMSOL identical to that shown in Figure 1b.

Afterward, we carry out a simulation of heat transfer to study the temporal change of the Ge$_2$Sb$_2$Te$_5$ layer’s temperature under a biasing voltage of 20 V. The material thermoelectric properties for Ge$_2$Sb$_2$Te$_5$, Au, and BK7 substrates used for the simulation are summarized in Supplementary Section S4. Figure 7a shows that the temperature in the Ge$_2$Sb$_2$Te$_5$ dielectric layer in the amorphous state increases with the time of adding the biasing voltage of 20 V. It goes beyond the amorphous to crystalline phase change temperature of 433 K after 2.6 μs. The 3D temperature distribution of the structure at 2.6 μs is shown in Figure 7b. One can observe that the whole amorphous Ge$_2$Sb$_2$Te$_5$ dielectric layer can exceed the transition temperature of 433 K after 2.6 μs, whereas the maximum temperature around 498 K is within the gap of the bow-tie antenna.

**CONCLUSION**

In conclusion, a method for ultrafast reversible manipulation of DQ-FR-induced lateral force created by an asymmetric BNA based on Au/Ge$_2$Sb$_2$Te$_5$ dual layers has been illustrated. We have presented that, by introducing a broken symmetry into the BNA, the Fano interaction between dipole and quadrupole modes results in a sideways force exerted on the dielectric nanoparticle. Such a Fano interference conservative force may laterally drag the particle in the opposite direction upon switching the state of Ge$_2$Sb$_2$Te$_5$ between amorphous and crystalline. A model of heat transfer is performed to determine the change of transient temperature in the asymmetric BNAs through an electric–thermal process. Our numerical simulation envisages that a short phase change time of 2.6 μs can be obtained with a low pumping intensity of 10 mW/μm$^2$, leading to an ultrafast position control of the nanobeads. Flexible manipulation of the magnitude and direction of the $F_r$ (lateral force) paves the way for observing collective phenomena of nano-objects and may be harnessed to afford a new twist of self-adaptive and active nano-optomechanical devices based on chalcogenide glass.
Further details on the Fano model fit of $F_s$ and material thermoelectric properties (PDF)
Supporting movie 1 (AVI)
Supporting movie 2 (AVI)

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