Selectively Plasmon-Enhanced Second-Harmonic Generation from Monolayer Tungsten Diselenide on Flexible Substrates

Zhuo Wang,†‡§¶ Zhaogang Dong,∥¶ Hai Zhu,¶ Lei Jin,† Ming-Hui Chiu,∇ Lain-Jong Li,∇ Qing-Hua Xu,† Goki Eda,‡⊥ Stefan A. Maier,§ Andrew T. S. Wee,*,†‡§○ Cheng-Wei Qiu,*,†‡§○ and Joel K. W. Yang*†∥◆

†NUS Graduate School for Integrative Sciences and Engineering (NGS), National University of Singapore, 28 Medical Drive, Singapore117456, Singapore
‡Department of Physics, National University of Singapore, 2 Science Drive 3, Singapore 117542, Singapore
§Department of Physics, Imperial College London, London SW7 2AZ, United Kingdom
∥Institute of Materials Research and Engineering, Agency for Science, Technology, and Research (A*STAR), 2 Fusionopolis Way, #08-03 Innovis, Singapore 138634, Singapore
¶Department of Chemistry, National University of Singapore, 3 Science Drive 3, Singapore 117543, Singapore
#Department of Electrical and Computer Engineering, National University of Singapore, 4 Engineering Drive 3, Singapore 117583, Singapore
∇Physical Science and Engineering Division, King Abdullah University of Science and Technology, Thuwal 23955−6900, Kingdom of Saudi Arabia
○Centre for Advanced 2D Materials, National University of Singapore, 2 Science Drive 3, Singapore 117542, Singapore
◆Singapore University of Technology and Design, 8 Somapah Road, Singapore 487372, Singapore

Supporting Information

ABSTRACT: Monolayer two-dimensional transition-metal dichalcogenides (2D TMDCs) exhibit promising characteristics in miniaturized nonlinear optical frequency converters, due to their inversion asymmetry and large second-order nonlinear susceptibility. However, these materials usually have very short light interaction lengths with the pump laser because they are atomically thin, such that second-harmonic generation (SHG) is generally inefficient. In this paper, we fabricate a judiciously structured 150 nm-thick planar surface consisting of monolayer tungsten diselenide and sub-20 nm-wide gold trenches on flexible substrates, reporting ~7000-fold SHG enhancement without peak broadening or background in the spectra as compared to WSe2 on as-grown sapphire substrates. Our proof-of-concept experiment yields effective second-order nonlinear susceptibility of 2.1 × 10⁴ pm/V. Three orders of magnitude enhancement is maintained with pump wavelength ranging from 800 to 900 nm, breaking the limitation of narrow pump wavelength range for cavity-enhanced SHG. In addition, SHG amplitude can be dynamically controlled via selective excitation of the lateral gap plasmon by rotating the laser polarization. Such a fully open, flat, and ultrathin profile enables a great variety of functional samples with high SHG from one patterned silicon substrate, favoring scalable production of nonlinear converters. The surface accessibility also enables integration with other optical components for information processing in an ultrathin and flexible form.

KEYWORDS: two-dimensional materials, second-harmonic generation, gap plasmon, transition-metal dichalcogenides, tungsten diselenide (WSe₂), sub-20 nm nanostructures
important role in frequency up-conversion in lasers and optoelectronic hybrid devices.\textsuperscript{5–7} As newly emerging nonlinear materials, two-dimensional transition-metal dichalcogenides (2D TMDCs),\textsuperscript{8} especially tungsten diselenide (WSe\textsubscript{2}),\textsuperscript{9} have attracted tremendous interest as they possess broken inversion-symmetry and relatively large second-order nonlinear susceptibility ($\chi^{(2)}$) despite being one monolayer thick.\textsuperscript{10–12} $\chi^{(2)}$ for monolayer TMDCs ranges from 5 to 500 pm/V depending on the excitation wavelength\textsuperscript{13} and sample quality.\textsuperscript{2} Thus, developing 2D TMDCs as a nonlinear optics source fulfills the demand for smaller and thinner nonlinear optical and optoelectronic devices.\textsuperscript{14–17} However, being atomically thin, 2D TMDCs also possess short light–matter interaction lengths, limiting the total SHG conversion efficiency.

In literature, there are preliminary reports of SHG enhancement in 2D TMDCs. For example, exciton-enhanced SHG, that is, the enhancement of SHG efficiency at the exciton resonance energy, has been demonstrated.\textsuperscript{15,18–21} At cryogenic temperatures, SHG intensity from monolayer WSe\textsubscript{2} can be tuned by changing the wavelength of the pump laser, and it is enhanced by 3 orders of magnitude when the excitation is two-photon resonant with the exciton energy.\textsuperscript{16} Nano-\textsuperscript{22} or microcavities\textsuperscript{23} have been demonstrated to enhance SHG in TMDCs at room temperature with enhancements varying from tens to thousands. The enhancement is attributed to the increased electromagnetic wave density achieved by aligning the pump wavelength with the cavity mode.\textsuperscript{22,23} However, these cavities made of semiconducting or dielectric materials are not suitable for ultrathin and flexible devices. Nevertheless, by fabricating subwavelength nanostructures patterned on flat surfaces, optical elements can be “flattened” into a 2D sheet of less than one wavelength thickness.\textsuperscript{26–29} In the context of developing planar and ultrathin optical devices, there is a compelling case to use ultrathin nanostructures to enhance the SHG of 2D TMDCs.

In this paper, we present a WSe\textsubscript{2}-gold nanostructure substrate consisting of a subwavelength structure in the form of sub-20 nm-wide trenches on a 150 nm-thick gold film, upon which monolayer WSe\textsubscript{2} is transferred. This WSe\textsubscript{2}-gold trench sample exhibits a significantly larger SHG signal at room temperature with an enhancement factor of \textasciitilde 7000, as compared to bare WSe\textsubscript{2} on sapphire substrates. This value is among the highest SHG enhancement factors for TMDCs reported thus far, corresponding to an effective second-order nonlinear susceptibility $\chi^{(2)}$ of $2.1 \times 10^4$ pm/V. The enhancement is attributed to the enhanced localized near-field of the pump laser at the sub-20 nm-wide trenches, boosting the SHG from the monolayer WSe\textsubscript{2}. Furthermore, this design allows for easy tuning of the total SHG intensity by rotating the linear polarization of the pump laser. Regardless of the pump laser polarization, the SHG spectra maintain the sharp peak profile of the pump laser. This hybrid nanostructure of monolayer WSe\textsubscript{2} on gold trenches is flat and mechanically flexible, with potential for further development of on-chip strain-induced tuning of bendable photonic devices.

RESULTS AND DISCUSSION

Flexible Nonlinear Devices Based on Hybrid Nanostructure of WSe\textsubscript{2}-Gold Trenches. Inversion symmetry breaking\textsuperscript{7} in the crystal structure of monolayer 2H-type WSe\textsubscript{2} brings about nonzero $\chi^{(2)}$, enabling WSe\textsubscript{2} to support SHG. Hybrid nanostructure, which consists of monolayer WSe\textsubscript{2} on a thin gold substrate patterned with sub-20 nm-wide trenches, was prepared to achieve high SHG (Figure 1a). The gold substrate with thickness of 150 nm was prepared by the template-stripping method.\textsuperscript{6} The monolayer WSe\textsubscript{2} flakes were grown on sapphire substrates by a chemical vapor deposition (CVD) method and then immediately transferred onto a freshly prepared gold substrate with sub-20 nm-wide trenches by a wet transfer technique (see details in Methods section). The quality and layer number of WSe\textsubscript{2} were determined by using optical microscopy (OM), Raman and photoluminescence before transfer (see details in Figure S1). The trenches used here are all aligned along one orientation (Figure S2a) such that the pump laser with electric field polarized perpendicularly to this orientation will excite gap plasmons within the trenches. Conversely, no plasmon excitation is expected when the pump laser is parallelly polarized. Therefore, tuning the polarization direction of the pump laser can switch ON or OFF the gap plasmons in the trenches, thus tuning the SHG intensity of WSe\textsubscript{2}.

The SHG measurement was conducted by using a femtosecond laser beam generated from a Ti-sapphire oscillator (Coherent, Chameleon Ultra II) with a central wavelength of
800 nm, pulse duration of 140 fs, and repetition rate of 80 MHz. The experiment of SHG as a function of pump wavelengths in Figure S10 was using this laser with a central wavelength of 800, 825, 850, 875, and 900 nm, respectively. The sample was normally illuminated by the pump laser via a 100× microscope objective lens with a numerical aperture (NA) of 0.90 (Nikon, Ti-U inverted microscope, TU Plan Fluor) and raster scanned by a piezo-actuated 3D nano-positioning stage. At each pixel, the backscattered SHG signal was collected through the same objective and sent to either a photomultiplier tube (PMT) (PicoQuant, PMA 182) or a spectrometer (Princeton Instruments, 2300i). More details about the optical setup can be seen in Methods, Figure S3, and Supplementary Note 1. Only in the experiments to investigate the orientations of WSe₂ crystal and trenches, an analyzer was placed before the detectors. Otherwise, the total SHG intensity was not influenced by the crystal orientation of the monolayer WSe₂. The SHG intensity was compared by taking peak values at 400 nm recorded by both PMT and spectrometer. Monolayer WSe₂ over trenches has SHG enhanced by up to ∼7000-fold as compared with WSe₂ on sapphire.

Unlike previously reported nanocavities or nanostructures, multiple gold nanostructures can be produced from one patterned silicon substrate, favoring scalable production. Moreover, the 150-nm-thick hybrid nanostructures provide a flat and flexible top surface, and they serve as an important nonlinear converter for realizing ultrathin and bendable optical information processors on chip. To test the feasibility, the hybrid nanostructure of WSe₂ on the gold substrate, which was weakly attached to a glass slide via optical adhesive glue, was peeled off from the glass slide using tweezers and transferred to a polydimethylsiloxane (PDMS) substrate of 1 mm thickness (see fabrication process in Figure S2). The macro shots, scanning electron micrographs (SEM) and SHG intensity of the sample were carefully compared before and after bending. The photo of the unbent sample clearly shows regions with patterned nanostructures on the gold film (see Figure 1a). Owing to its nanoscale thickness (∼150 nm) and intrinsic flexibility, the hybrid nanostructure can be bent outward (Figure 1b) and inward (Figure S4) repeatedly in a controllable way once attached to the PDMS substrate. As the PDMS substrate was bent outward ∼40° off the horizontal line with a bending radius of 2.8 mm, the trenches were expanded along the width direction. As a result, the width of trenches on the bent sample (∼17 nm) is slightly larger than that on the unbent sample (∼15 nm) (see Figure 1c,d). As shown in Figure 1e,f, compared with the unbent sample, the bend does not dramatically affect the SHG intensity of WSe₂ on trenches. It is found that after being bent inward and outward for 50 times, the sample can still maintain 70% of the SHG intensity as the unbent one (Figure S5). For simplicity in handling the samples, the characterization below was conducted on flat samples adhered to glass substrates.

**Giant SHG Enhancement.** To experimentally demonstrate that the SHG from the trenches is significantly enhanced, we transferred a monolayer single-crystalline triangular WSe₂ flake on gold trenches spaced at a large pitch of 910 nm. This large pitch of 910 nm allows us to have the clear mapping of the SHG intensity from the sub-20 nm-wide trench region, based on the far-field optical characterization setup (see Figure S3). Figure 2a shows the SEM image of a triangular single-crystalline WSe₂ flake covering 6 trenches. Figure 2b presents the simulated electric field distributions over one of these trenches with pump polarization perpendicular (left panel) and parallel (right panel) to the trench. Corresponding to the SEM image, there are 6 brighter SHG stripes in the SHG mapping (Figure 2c) when the polarization direction of incident light is perpendicular to the trench orientation, showing that the SHG enhancement position is localized within the trenches that support lateral gap plasmons. This observation can be corroborated by the simulated localized electric field distribution over the trenches with the pitch of 910 nm (left panel in Figure 2b). As expected, when the incident light is rotated by 90°, SHG signal from the trenches significantly decreases (Figure 2d), that is, trenches without the excitation of lateral gap plasmons (right panel in Figure 2b) have little influence on SHG from WSe₂.

To achieve giant SHG enhancement, we optimized the pitch sizes of the gold nanostructures. The giant SHG intensity was achieved from WSe₂ suspended over the trench with a pitch of 170 nm. At the 170 nm pitch size, the lateral gap plasmon resonance is aligned with pump laser wavelength of 800 nm. Figure 3a presents the SEM image of the sample, where a monolayer WSe₂ flake is covering both the trench (dark gray) and flat gold film (gray) regions. Figure 3b presents the reflectance spectra of the gold trenches (T and T') and flat gold film (F and F') respectively, for both x and y polarizations (see details in Methods section for the reflectance spectrum measurement). The reflectance spectra of the flat gold film (F and F') show no polarization dependence (black and orange lines) as expected due to the isotropic optical properties of gold in the x–y plane. In comparison, the polarization of incident light can turn ON or OFF the lateral gap plasmons in the trenches. Specifically, x-polarized incident light excites the lateral gap plasmon resonance seen as the broad absorption dip at ∼800 nm in the reflectance spectrum (T, red line). In
Figure 3. Maximum SHG enhancement from WSe2 on trenches with plasmon resonance aligned with 800 nm pump laser. (a) SEM image of a monolayer WSe2 flake on gold trenches with pitch of 170 nm (dark gray) denoted as T(T′) and flat gold film (gray) denoted as F(F′). White dashed line outlines the edges of WSe2. The blue dashed line outlines the boundary of trenches and flat gold film. (b) Reflectance spectra of gold trenches (T or T′) and flat gold film (F or F′) under the illumination of white light polarized perpendicular (x) or parallel (y) to the trenches orientation. The gold trenches have lateral gap plasmon resonance at ~800 nm under the illumination of x-polarized light. (c) PL and (d) Raman intensity mappings of the WSe2 flake on gold trenches and flat gold film. The intensity value at each pixel for PL mapping was obtained by integrating the PL spectrum across the spectrum window of 700–820 nm, for Raman was the spectrum window of 245–265 cm−1. (e,f) SHG peak intensity mapping of WSe2 on gold trenches (T and T′) and flat gold film (F and F′) under resonant and nonresonant excitations, respectively. The pump laser is 800 nm with a power of 0.5 mW.

contrast, y-polarized incident light with electric field of being polarized along the trench direction cannot excite gap plasmons and exhibits a similar reflectance spectrum as the flat film (T′, blue line). The former polarization case is referred to as “resonant excitation” with capital letters representing each sample (T for trenches, F for flat gold, or S for sapphire) and the latter “non-resonant excitation” with apostrophe (T′, F′, or S′) for simplicity. The dips at ~400 and ~470 nm in all reflectance spectra are attributed to the absorption in gold caused by interband transitions.32

The uniformity of the WSe2 flake is reflected in the uniform intensities in the PL (Figure 3c) and Raman mappings (Figure 3d). In addition, its monolayer nature is confirmed by the related spectra (Figure S1e,f), where the PL peak at ~750 nm and Raman spectrum of two dominant peaks at ~250 cm−1 are indicative of monolayer WSe2. The lateral gap plasmon plays a significant role in enhancing SHG conversion efficiency. Figure 3e,f shows the SHG mappings of WSe2 on gold trenches and flat gold film. The 800 nm pump laser was incident normally to the surface and polarized along x-axis (Figure 3e) and y-axis (Figure 3f), respectively. As the SHG signal was collected without any analyzer in front of the detector, the total SHG intensity was independent of the crystal orientation of WSe2 with respect to the polarization direction of pump laser. Furthermore, the trenches without WSe2 as shown in the SEM image (Figure S6a) show no observable SHG signal (Figure S6b), indicating that the measured SHG signal is only from the SHG-active material WSe2. Furthermore, the surface non-linearity of flat gold was insignificant.5,33

The as-grown WSe2 on sapphire was taken as the reference sample. As shown in the SHG mapping (Figure S1d), monolayer WSe2 on sapphire has a uniform SHG intensity distribution over the flake. For a quantitative comparison, 4 SHG spectra from WSe2 on the gold trenches (T or T′) and sapphire (S or S′) under x- or y-polarized excitation conditions are shown in Figure 4a. Under resonant excitation, the SHG peak value from monolayer WSe2 flake on trenches (T) is enhanced by ~900-fold on average relative to the reference sample (S). As observed in both simulation and experiments in Figure 2, the SHG enhancement of the sample originates from the trenches. Accounting for the small area fraction (12.6%) of trenches within the laser spot, the maximum SHG enhancement of WSe2 over the trenches is calculated to be ~7000-fold. Details of the normalization method are discussed in Figure S7 and Supplementary Note 2. The enhancement arises from the lateral gap plasmon with concentrated electric field in the plane of WSe2, increasing the light–matter interaction and enabling the WSe2 flake to more effectively convert 800 nm light into 400 nm light.

Rotating the polarization of pump laser will dynamically tune the total SHG intensity of WSe2 on gold trenches with an extinction ratio of ~47 (top panel, Figure 4a). At the nonresonant excitation condition, the SHG intensity (T′) drops to ~1/47 of the counterpart at resonant excitation condition (T) with an enhancement factor of <150, owing to the absence of gap plasmons. As expected, no polarization dependence was seen in WSe2 on sapphire (bottom panel, Figure 4a). This conclusion is also verified by the SHG intensity extracted from the SHG mappings (see Figure 4b).

Figure 4. Quantitative comparison of SHG intensity. (a) Representative SHG spectra from WSe2 on gold trenches (T or T′) and sapphire (S or S′) measured by using x- or y-polarized pump laser, respectively. (b) SHG peak intensity with an error bar of WSe2 on gold trenches and on sapphire. Ten data points were directly collected from the SHG mapping for each position without normalization of the trench area. The “7000” and “150” denote the normalized SHG enhancement factor under resonant and nonresonant excitations, respectively, where WSe2 on sapphire was used as reference. (c) Finite-difference time domain (FDTD) simulation of the electric field distribution of the lateral gap plasmons with a WSe2 monolayer flake being suspended over a single trench with a maximum width of ~18 nm and a pitch of 170 nm. The polarization of the incident laser field is across the gap. The dashed yellow line denotes the boundary between air and gold.
SHG Enhancement Mechanism. For a monolayer WSe₂ with $D_{3h}$ (6m2) point-group symmetry, the second-order nonlinear susceptibility tensor has the following nonzero elements:

$$\chi^{(2)}_{WSe_2} = \chi^{(2)}_{bab} = -\chi^{(2)}_{bub} = -\chi^{(2)}_{abu} = \chi^{(2)}_{baa}$$

where $a$ and $b$ are the principle axes in crystal coordinates. Here, $a$ corresponds to the zigzag direction and $b$ corresponds to the armchair direction that is parallel to a vertical mirror plane (Figure S9). This symmetry leads to a theoretical estimate of the total SHG signal:

$$I_{2\omega} = C|E_{2\omega}|^2 \propto |\chi^{(2)}_{bab}|^2 |E_{\omega}|^4$$

where $E_{2\omega}$ is the electric field of the second-harmonic frequency wave, $E_{\omega}$ is the electric field of the pump laser, and $C$ is a constant (see eq S16). The gold trenches are designed to enhance the nonlinear effects of WSe₂ by providing near-field enhancement of the pump laser ($E_\omega$) at the trenches via the excitation of lateral gap plasmons. Figure 4c shows the simulated near-field distribution over a trench with a pitch of 170 nm, where the spatial overlap between the enhanced near field of $E_\omega$ and monolayer WSe₂ strengthens the light coupling in WSe₂ and thus the SH emission. Quantitatively, the near-field of $E_\omega$ is enhanced by $\sim$13-fold as compared to the electric field of the incident pump laser ($E_0$) and thus predicting a theoretical SHG enhancement factor of $13^4 \sim 28,000$. Our SHG enhancement factor, $\sim 7000$, obtained by using WSe₂ on sapphire as a reference is only 25% of the predicted value owing to the partial absorption of the SHG signal at 400 nm by the gold substrate and partial absorption of the pump at 800 nm caused by the energetic proximity of the exciton in WSe₂ with the pump. The reabsorption of the 400 nm signal can be seen in the reflectance spectrum of gold trenches (Figure 3b). Note that the trenches have a spectrally broad lateral gap plasmon resonance and extremely narrow mode volume thus having large electric field enhancement for pump with wavelength ranging from 800 to 900 nm. As a result, at this wide pump range, the SHG enhancement factor is maintained at thousands-fold for WSe₂ on trenches (Figure S10). In addition, our method applies to enhance SHG of various 2D materials such as monolayer MoS₂ and MoSe₂ with an enhancement factor of thousands-fold (Figure S11).

The effective second-order nonlinear susceptibility $\chi^{(2)}_{eff}$ was computed using the measured SHG spectra according to the formula:

$$\chi^{(2)}_{eff} \propto (I_{2\omega})^{1/2} / I_{\omega}$$

where $I_\omega$ and $I_{2\omega}$ are the pump laser and second-harmonic intensities, respectively. According to this method, the effective second-order nonlinear susceptibility $\chi^{(2)}_{eff}$ of WSe₂ on gold trenches is calculated to be $\sim 2.1 \times 10^4$ pm/V with normalization of the trench occupation. In contrast, the effective $\chi^{(2)}_{eff}$ of our CVD-grown WSe₂ on sapphire is $\sim 248$ pm/V, which is on the same order as reported values. More detail about the calculation of $\chi^{(2)}_{eff}$ can be seen in the Supplementary Note 3.

Polarization-resolved SHG measurements provide important crystallographic information on WSe₂ atomic layers if the signal is collected through a linear polarized-analyzer set, due to the sensitivity of the SHG to crystal symmetry. To determine and distinguish the contributions of SHG signals influenced by the monolayer WSe₂ crystal orientation and the trench orientation, a single crystalline monolayer WSe₂ flake covering both gold trenches (I) and flat gold film (II) was measured (Figure 5a). The pump laser was polarized along the $y$ axis, and the parallel SHG signal was collected, that is, also along the $y$ axis, where the sample was rotated clockwise by an angle of $\theta$ in steps of $5^\circ$. The trenches were initially aligned with the $x$ axis, and the offset angle between the armchair axis of the WSe₂ flake and $y$ axis was $\theta_0$. The polar plots for SHG of WSe₂ on gold trenches
(Region I) and on flat gold (Region II) are shown in Figure S5b and Figure S12a, respectively, where the SHG intensity is plotted as a function of the rotation angle \( \theta \) of the sample. A typical petal pattern with 6-fold symmetry is observed (Figure S12a and Supplementary Note 4) for WSe\(_2\) on flat gold where the SHG pattern is fitted with an equation:

\[
t I_{\text{sh}, \text{WSe}_2 \text{on flat gold}} = C_1 \cos^2[3(\theta + \theta_0)]
\]

(4)

where \( C_1 \) is a constant obtained from the largest SHG intensity. The peaks of SHG intensity point to the armchair directions in monolayer WSe\(_2\) lattice, that is, the perpendicular bisectors of the single crystalline flake (blue dashed arrow). The fitting shown in red shows that the initial offset angle \( \theta_0 \) between the armchair direction of the single crystalline WSe\(_2\) and pump laser polarization is 10°, indicating that the armchair axis was initially rotated with respect to the pump laser. Unlike the polar pattern of Region II, Region I shows a polar pattern with two large and two small petals (Figure S5b) that can be fitted by the equation:

\[
t I_{\text{sh}, \text{WSe}_2 \text{on the trenches}} = C_2 \cos^2[3(\theta + \theta_0)] \times \cos^2 \theta
\]

(5)

where \( C_2 \) is a constant that fits the SHG amplitude at each angle (see eq S20). The first cosine term represents the influence of the crystal orientation, and the second cosine term reflects how the angle between the trench and the \( x \) axis influences the SHG intensity. The trenches were initially oriented perpendicular to the polarization of pump laser, in which case, the near field of the pump laser localized at the gap has the largest value: \( E_{\text{gap, initial}}^\parallel \parallel E_{\text{gap}} \) where \( E_{\text{gap}} \) is the enhanced local electric field with the same polarization direction as \( E_{\text{gap}} \) and \( f \) is the enhancement factor defined by \( E_{\text{gap}}/E_{\text{a}} \). As the trenches rotate by angle \( \theta \), the near field enhanced by the gap plasmon along the direction of pump laser is given by \( E_{\text{gap, rotated}}^\parallel = f E_{\text{a}} \cos \theta \) (Figure S13). Therefore, the SHG intensity of the WSe\(_2\) on gold trenches varies with the rotation of the trench according to the \( \cos^2 \theta \) function. More details can be seen in the Supporting Note 5 and Figure S13.

The components of the second-order nonlinear susceptibility are provided in terms of the crystal axes \((a, b, c)\) as discussed in eq 1. However, it is convenient to describe the nonlinear polarization in terms of the laboratory axes \((x, y, z)\) as the direction of propagation and polarizations of the interacting waves are defined relative to the laboratory axes. According to the transformation from the crystal coordinate to the laboratory coordinate, we can derive the effective second-order nonlinear susceptibility along \( x \) and \( y \) axes (see details in Figure S9 and the corresponding detailed description in Supporting Note 4). The parallel \( (E_{\text{parallel}}^\parallel) \) and perpendicular \( (E_{\text{perpendicular}}^\perp) \) components of the second-harmonic electric field with respect to the pump laser polarization \((y \text{ axis})\) can be expressed via the effective second-order nonlinear susceptibility:

\[
E_{\text{parallel}}^\parallel \propto |\psi_{\text{666}}^{(2)}| \cos 3(\theta + \theta_0)
\]

(6)

\[
E_{\text{perpendicular}}^\perp \propto |\psi_{\text{666}}^{(2)}| \sin 3(\theta + \theta_0)
\]

(7)

The fitting curves for the polarization-dependent SHG in Figure S5b and Figure S12b are consistent with the theoretical verification of eq 6. The total SHG intensity (without the analyzer) is expressed as follows:

\[
I_{2\omega} \equiv I_{2\omega}^\parallel + I_{2\omega}^\perp = C_i^2 \left[ (E_{2\omega}^\parallel)^2 + (E_{2\omega}^\perp)^2 \right] \propto C_i^2 |\psi_{\text{666}}^{(2)}|^2
\]

(8)

where \( I_{2\omega} \) is constant with respect to the crystal orientation. Therefore, the crystal orientation influences the parallel or perpendicular component of SHG signal, but not the total SHG signal.

The power-dependent total SH signals from both WSe\(_2\) on gold trenches (Figure S5c) and on flat gold film (Figure S12b) exhibit a quadratic input power dependence, and the fitting line (red) has a slope of ~2, in agreement with the second-order nature of the nonlinear process. As shown in Figure S5c, the experimental results (black squares) deviate from the fitting line (red) at higher excitation power and show a shallower slope with increasing pump power, indicating saturation in SHG.\(^{40,41}\)

CONCLUSION

In summary, we present a hybrid nanostructure consisting of WSe\(_2\) on a gold film with trenches that support lateral gap plasmon resonances at ~800 nm. The hybrid nanostructure is flexible and significantly enhances second-harmonic emission at 400 nm by ~7000-fold, without emission peak broadening or increased spectral background at room temperature. As observed in both experiments and simulation, the augmented SHG is attributed to the enhancement of the local excitation fields within the sub-20 nm-wide trenches. Furthermore, the anisotropic gold substrate composed of trenches aligned along a single direction allows for dynamic tuning of the SHG amplitude from WSe\(_2\) by simply rotating the polarization direction of the pump laser. This hybrid nanostructure provides a convenient and practical approach to obtain blue emission from a near-infrared laser in monolayer TMDCs. Furthermore, it provides a proof-of-concept for ultrathin and flexible frequency converters with high monochromaticity, realizing a miniaturized bendable photonic device for various applications, for example, information processing, and providing a new freedom of engineering the optical properties of WSe\(_2\) by strain imposed by the bendable substrate.\(^{42}\)

METHODS

Material Growth and Quality of WSe\(_2\). The monolayer WSe\(_2\) single crystal was grown on c-cut sapphire by a chemical vapor deposition (CVD) of WO\(_3\) and Se powders in a horizontal hot-wall chamber. The WO\(_3\) powders at the center heating zone were heated to 925 °C, and the Se powders at the upper stream side were maintained at 270 °C. The WSe\(_2\) samples were obtained on sapphire substrate placed at the downstream side using an Ar/H\(_2\) flow at 10 Torr for 15 min. The detailed growth procedures can be found elsewhere.\(^{43,44}\) This technique yields high-quality monolayer WSe\(_2\) with a crystal size ranging from 4 to 15 μm (Figure S1a). The typical PL spectrum of a pristine monolayer WSe\(_2\) (Figure S1e) is dominated by an emission peak at 765 nm (1.62 eV) that arises from the A direct excitonic transition.\(^{45,46}\) For monolayer WSe\(_2\) on sapphire, the Raman spectrum excited by a 532 nm laser, shown in Figure S1f, has two characteristic peaks are at 250 and 259 cm\(^{-1}\) that originate from the degenerate E'/A'\(_1\) mode and 2LA(M) mode, respectively.

Fabrication of Gold Substrate and Transferring of WSe\(_2\). The gold substrate consisting of gold trenches and flat gold film was prepared by a template-stripping method based on nanopatterned silicon templates.\(^{6,44}\) First, hydrogen silsesquioxane (HSQ) was spin coated onto a cleaned silicon substrate and then was patterned by electron beam lithography (EBL). After development of the exposed HSQ, silicon etching and HSQ mask removal were carried out. Next, a 150 nm-thick gold film was evaporated onto the silicon substrate, followed by a template-stripping process with a glass slide. More details are in the Supporting Information. WSe\(_2\) flake was then transferred onto the gold substrate by a wet transfer approach.\(^{44,47}\) A layer of poly(methyl methacrylate) (PMMA) (950 K AS) was first spin
coated on the monolayer WSe₂ flakes as a transfer supporting layer and then baked at 130 °C for 2 min. The PMMA capped WSe₂ was exfoliated from the sapphire substrate in a NaOH solution (3 mol/L) at 100 °C. After dilution of etchant and residues in deionized water, the PMMA-capped monolayer WSe₂ was transferred onto the gold substrate, followed by the removal of PMMA film using acetone and sample cleaning by isopropyl alcohol. For making flexible devices, the gold substrate with WSe₂ was peeled off from the glass slide by a tweezer and pasted onto a sticky bendable polydimethylsiloxane (PDMS) substrate (Figure S2).

Characterization. Otherwise stated specifically, the characterization was conducted on un bent samples. AFM images were obtained using a BRUKER Dimension FastScan equipment. The optical reflectance spectra of the samples were measured by using a CRAIC UV-vis-NIR microspectrophotometer model QD1 2010 (equipped with a 365 nm objective lens with NA of 0.5). Moreover, SEM images were obtained by FEI Verios 460. A confocal microphotoluminescence/Raman setup was used to excite the sample using a 532 nm CW pump laser, which was focused by a 100× microscope objective lens. The SHG was measured by a femtosecond laser beam with a central wavelength of 800, 825, 850, 875, or 900 nm, a pulse duration of 140 fs, and a repetition rate of 80 MHz at room temperature. The detailed setup is shown in Figure S3. There was no analyzer before the detectors except in the experiment of investigating the influence of crystal and trench orientation. Therefore, the total SHG intensity shown in Figures 1e, 1f, 2c, 2d, 3a, 3b, Figure 5c and Figures S1, S5, S6, S8, S10, S11, and S12b does not depend on the crystal orientation, while the parallel component of SHG intensity relative to the polarization of pump laser shown in Figure 5b and Figure S8a is related to the crystal orientation. We considered and experimentally calibrated the change of the S- and P-polarized light caused by optical components such as dichroic mirror and short pass, and the detecting sensibility of the spectrometer and PMT. For all SHG measurements, the pump laser power on the sample was typically set at 0.5 mW, far below the saturation region, to prevent possible damage, with the exception of the experiment on power dependence in Figure 5c and Figure S12b. In addition, the SHG enhancement factor is defined by the ratio of the total SHG intensity from TMDCs on the trenches region to that from TMDCs on sapphire.

Numerical Simulations. A commercial software package, Lumerical FDTD Solutions, was used to simulate the electric field amplitude as a function of the rotation angle θ of the trenches (Figure S13); Height of the ridges on silicon template (Figure S14) (PDF)

ASSOCIATED CONTENT

Supporting Information
The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsnano.7b08682.

Characterization results of WSe₂ on sapphire, flat gold, and the gold trenches (Figure S1); Detailed illustration on the fabrication process of flexible hybrid structure (Figure S2); Optical setup for measuring SHG mappings and SHG spectra at room temperature (Figure S3); Photograph of WSe₂ on gold substrate attached to an inward-bent polydimethylsiloxane (PDMS) substrate (Figure S4); SHG spectra of the sample (WSe₂ on nanostructure with a pitch of 170 nm) before and after being bent 50 times (Figure S5); Gold trenches without WSe₂ has no SHG (Figure S6); Diagram showing the area of multiple trenches perpendicular to the polarization direction of the laser within a laser spot (Figure S7); Comparing spectra profile of second harmonic generation with central wavelength of 400 nm (SHG, red line, bottom axis) and fundamental wave (FW, black dot, top axis) with central wavelength of 800 nm (Figure S8); Demonstration of transformation from crystal coordinates (a, b, c) to laboratory coordinates (x, y, z) (Figure S9); SHG intensity from monolayer WSe₂ on trenches with a pitch of 170 nm and on sapphire as a function of pump wavelength ranging from 800 to 900 nm (Figure S10); Quantitative comparison of SHG from monolayer WSe₂, MoSe₂, and MoS₂ on nanostructure with a pitch of 170 nm and on the as-grown sapphire (Figure S11); Dependence of the SHG on sample rotated angle, laser power, and pump wavelength on SHG intensity, respectively (Figure S12); Demonstration of the electric field amplitude as a function of the rotation angle θ of the trenches (Figure S13); Height of the ridges on silicon template (Figure S14) (PDF)

AUTHOR INFORMATION

Corresponding Authors
*E-mail: joel_yang@sutd.edu.sg.
*E-mail: chengwei.qiu@nus.edu.sg.
*E-mail: phyweets@nus.edu.sg.

ORCID
Zhaoqiang Dong: 0000-0002-0929-7723
Goki Eda: 0000-0002-1575-8020
Cheng-Wei Qiu: 0000-0002-6605-500X
Joel K. W. Yang: 0000-0003-3301-1040

Author Contributions

Notes
The authors declare no competing financial interest.

ACKNOWLEDGMENTS

Z.W. acknowledges scholarship support from NUS Graduate School for Integrative Sciences and Engineering (NGS). Z.D. and J.K.W.Y. acknowledge the funding support from the Agency for Science, Technology, and Research (A*STAR) Young Investigatorship (grant number 0926030138), SERC (grant number 092154099), the National Research Foundation (grant number NRF-CRP 8-2011-07), A*STAR Pharos Program (Grant No. 1527300025), and A*STAR-JCO under project number 1437C00135. C.W.Q. acknowledges the financial support from A*STAR Pharos Program (grant no. 152.70 00014, with project no. R-263-000-R91-305). Z.W. and A.T.S.W. acknowledge the funding support from MOE Tier 2 grant R 144-000-382-112 and facility support from NUS Center for Advanced 2D Materials. S.A.M. acknowledges the EPSRC Reactive Plasmonics Programme grant (EP/M013812/1), the Royal Society, and the Lee-Lucas Chair in Physics. L.-J.L.

DOI: 10.1021/acsnano.7b08682
ACS Nano 2018, 12, 1859–1867
acknowledges support from KAUST (Saudi Arabia) and Taiwan Consortium of Emergent Crystalline Materials (TCECM). G.E. also acknowledges support by Ministry of Education (MOE), Singapore, under AcRF Tier 2 (MOE2015-T2-2-123).

REFERENCES

(31) Lee, J.; Tymchenko, M.; Argyropoulos, C.; Chen, P.-Y.; Lu, F.; Demmerle, F.; Boehm, G.; Amann, M.-C.; Ala, A.; Belkin, M. A. Giant


